



ASHLAWN  
SCHOOL

# A-Level Maths

## Y11-Y12 Transition

How to use this document:

- Use the contents page and any blue text to navigate the document.
- Read through the written examples.
- Complete the sets of practice questions.
- Use the corresponding video for each practice set to support and to self-assess.
- Complete additional practice, using the solutions at the end of the document to self-assess.

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## Indices

### Worked Examples

Simplify  $\frac{x^5}{x^2}$

$\frac{x^5}{x^2} = x^3$	use the rule $\frac{a^m}{a^n} = a^{m-n}$ to give $\frac{x^5}{x^2} = x^{5-2} = x^3$
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Simplify  $6x^6 \times 3x^4$

$6x^6 \times 3x^4 = 18x^{10}$	$6 \times 3 = 18$ and then use the rule $a^m \times a^n = a^{m+n}$ to give $x^6 \times x^4 = x^{6+4} = x^{10}$
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Simplify  $(x^4)^2 \times 3x^5$

$(x^4)^2 \times 3x^5 = 3x^{13}$	$3 \times 1 = 3$ and then use the rule $(a^m)^n = a^{mn}$ following by to give $a^m \times a^n = a^{m+n}$ $(x^4)^2 \times x^5 = x^{4 \times 2} \times x^5$ $= x^8 \times x^5$ $= x^{8+5}$ $= x^{13}$
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Evaluate  $9^{\frac{1}{2}}$

$9^{\frac{1}{2}} = \sqrt{9}$ $= 3$	Use the rule $a^{\frac{1}{n}} = \sqrt[n]{a}$
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Evaluate  $27^{\frac{2}{3}}$

$27^{\frac{2}{3}} = (\sqrt[3]{27})^2$ $= 3^2$ $= 9$	<b>1</b> Use the rule $a^{\frac{m}{n}} = (\sqrt[n]{a})^m$ <b>2</b> Use $\sqrt[3]{27} = 3$
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Evaluate  $4^{-2}$

$4^{-2} = \frac{1}{4^2}$ $= \frac{1}{16}$	<b>1</b> Use the rule $a^{-m} = \frac{1}{a^m}$ <b>2</b> Use $4^2 = 16$
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## Practice Questions

Set 1

Simplify these expressions:

**a.**  $x^2 \times x^5$    **b.**  $2r^2 \times 3r^3$    **c.**  $\frac{b^7}{b^4}$    **d.**  $6x^5 \div 3x^3$    **e.**  $(a^3)^2 \times 2a^2$    **f.**  $(3x^2)^3 \div x^4$

Set 2

Simplify:

**a.**  $\frac{x^3}{x^{-3}}$    **b.**  $x^{\frac{1}{2}} \times x^{\frac{3}{2}}$    **c.**  $(x^3)^{\frac{2}{3}}$    **d.**  $2x^{1.5} \div 4x^{-0.25}$    **e.**  $\sqrt[3]{125x^6}$    **f.**  $\frac{2x^2 - x}{x^5}$

Set 3

Evaluate:

**a.**  $9^{\frac{1}{2}}$    **b.**  $64^{\frac{1}{3}}$    **c.**  $49^{\frac{3}{2}}$    **d.**  $25^{-\frac{3}{2}}$

## Video Solutions

[Set 1](#)

[Set 2](#)

[Set 3](#)

## Additional Practice

Set 1

**1.** (a) Simplify  $a^4 \times a^5$

**2.** (a) Simplify  $x^7 \times x^3$

(b) Simplify  $\frac{45e^6 f^8}{5ef^2}$

(b) Simplify  $(m^4)^3$

(c) Write down the value of  $9^{\frac{1}{2}}$

(c) Simplify  $\frac{36af^8}{12a^5 f^2}$

Set 2

1 Simplify.

**a**  $\frac{3x^2 \times x^3}{2x^2}$

**b**  $\frac{10x^5}{2x^2 \times x}$

**c**  $\frac{3x \times 2x^3}{2x^3}$

**d**  $\frac{7x^3y^2}{14x^5y}$

**e**  $\frac{y^2}{y^{\frac{1}{2}} \times y}$

**f**  $\frac{c^{\frac{1}{2}}}{c^2 \times c^{\frac{3}{2}}}$

**g**  $\frac{(2x^2)^3}{4x^0}$

**h**  $\frac{x^{\frac{1}{2}} \times x^{\frac{3}{2}}}{x^{-2} \times x^3}$

Set 3

1 Evaluate.

**a**  $49^{\frac{1}{2}}$

**b**  $64^{\frac{1}{3}}$

2 Evaluate.

**a**  $25^{\frac{3}{2}}$

**b**  $8^{\frac{5}{3}}$

3 Evaluate.

**a**  $5^{-2}$

**b**  $4^{-3}$

4 Evaluate.

**a**  $4^{-\frac{1}{2}}$

**b**  $27^{-\frac{2}{3}}$

[Solutions](#)

## Surds

### Worked Examples

Simplify  $\sqrt{50}$

$\begin{aligned}\sqrt{50} &= \sqrt{25 \times 2} \\ &= \sqrt{25} \times \sqrt{2} \\ &= 5 \times \sqrt{2} \\ &= 5\sqrt{2}\end{aligned}$	<ol style="list-style-type: none"><li>1 Choose two numbers that are factors of 50. One of the factors must be a square number</li><li>2 Use the rule <math>\sqrt{ab} = \sqrt{a} \times \sqrt{b}</math></li><li>3 Use <math>\sqrt{25} = 5</math></li></ol>
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Simplify  $\sqrt{147} - 2\sqrt{12}$

$\begin{aligned}\sqrt{147} - 2\sqrt{12} \\ &= \sqrt{49 \times 3} - 2\sqrt{4 \times 3} \\ \\ &= \sqrt{49} \times \sqrt{3} - 2\sqrt{4} \times \sqrt{3} \\ &= 7 \times \sqrt{3} - 2 \times 2 \times \sqrt{3} \\ &= 7\sqrt{3} - 4\sqrt{3} \\ &= 3\sqrt{3}\end{aligned}$	<ol style="list-style-type: none"><li>1 Simplify <math>\sqrt{147}</math> and <math>2\sqrt{12}</math>. Choose two numbers that are factors of 147 and two numbers that are factors of 12. One of each pair of factors must be a square number</li><li>2 Use the rule <math>\sqrt{ab} = \sqrt{a} \times \sqrt{b}</math></li><li>3 Use <math>\sqrt{49} = 7</math> and <math>\sqrt{4} = 2</math></li><li>4 Collect like terms</li></ol>
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Simplify  $(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2})$

$\begin{aligned}(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2}) \\ &= \sqrt{49} - \sqrt{7}\sqrt{2} + \sqrt{2}\sqrt{7} - \sqrt{4} \\ \\ &= 7 - 2 \\ &= 5\end{aligned}$	<ol style="list-style-type: none"><li>1 Expand the brackets. A common mistake here is to write <math>(\sqrt{7})^2 = 49</math></li><li>2 Collect like terms: <math display="block">-\sqrt{7}\sqrt{2} + \sqrt{2}\sqrt{7} \\ = -\sqrt{7}\sqrt{2} + \sqrt{7}\sqrt{2} = 0</math></li></ol>
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Rationalise  $\frac{1}{\sqrt{3}}$

$\frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$ $= \frac{1 \times \sqrt{3}}{\sqrt{9}}$ $= \frac{\sqrt{3}}{3}$	<ol style="list-style-type: none"><li>1 Multiply the numerator and denominator by <math>\sqrt{3}</math></li><li>2 Use <math>\sqrt{9} = 3</math></li></ol>
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Rationalise and simplify  $\frac{3}{2+\sqrt{5}}$

$\frac{3}{2+\sqrt{5}} = \frac{3}{2+\sqrt{5}} \times \frac{2-\sqrt{5}}{2-\sqrt{5}}$ $= \frac{3(2-\sqrt{5})}{(2+\sqrt{5})(2-\sqrt{5})}$ $= \frac{6-3\sqrt{5}}{4+2\sqrt{5}-2\sqrt{5}-5}$ $= \frac{6-3\sqrt{5}}{-1}$ $= 3\sqrt{5}-6$	<ol style="list-style-type: none"><li>1 Multiply the numerator and denominator by <math>2-\sqrt{5}</math></li><li>2 Expand the brackets</li><li>3 Simplify the fraction</li><li>4 Divide the numerator by <math>-1</math> Remember to change the sign of all terms when dividing by <math>-1</math></li></ol>
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### Practice Questions

Set 1

Simplify:

a.  $\sqrt{12}$     b.  $\frac{\sqrt{20}}{2}$     c.  $5\sqrt{6} - 2\sqrt{24} + \sqrt{294}$

Set 2

Expand and simplify if possible:

a.  $\sqrt{2}(5-\sqrt{3})$     b.  $(2-\sqrt{3})(5+\sqrt{3})$

Set 3

Rationalise the denominator of:

a.  $\frac{1}{\sqrt{3}}$     b.  $\frac{1}{3 + \sqrt{2}}$     c.  $\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}}$     d.  $\frac{1}{(1 - \sqrt{3})^2}$

Video Solutions

[Set 1](#)

[Set 2](#)

[Set 3](#)

Additional Practice

Set 1

1 Simplify.

a  $\sqrt{45}$

b  $\sqrt{125}$

c  $\sqrt{48}$

d  $\sqrt{175}$

2 Simplify.

a  $\sqrt{72} + \sqrt{162}$

b  $\sqrt{45} - 2\sqrt{5}$

c  $\sqrt{50} - \sqrt{8}$

d  $\sqrt{75} - \sqrt{48}$

e  $2\sqrt{28} + \sqrt{28}$

f  $2\sqrt{12} - \sqrt{12} + \sqrt{27}$

Set 2

1 Expand and simplify.

a  $(\sqrt{2} + \sqrt{3})(\sqrt{2} - \sqrt{3})$

b  $(3 + \sqrt{3})(5 - \sqrt{12})$

c  $(4 - \sqrt{5})(\sqrt{45} + 2)$

d  $(5 + \sqrt{2})(6 - \sqrt{8})$

2 Expand and simplify  $(\sqrt{x} + \sqrt{y})(\sqrt{x} - \sqrt{y})$

3 Work out the value of  $(\sqrt{2} + \sqrt{8})^2$

4 Expand  $(1 + \sqrt{2})(3 - \sqrt{2})$

Give your answer in the form  $a + b\sqrt{2}$  where  $a$  and  $b$  are integers.



Set 3

1 Rationalise and simplify, if possible.

a  $\frac{1}{\sqrt{5}}$

b  $\frac{1}{\sqrt{11}}$

c  $\frac{2}{\sqrt{7}}$

d  $\frac{2}{\sqrt{8}}$

e  $\frac{2}{\sqrt{2}}$

f  $\frac{5}{\sqrt{5}}$

2 Rationalise and simplify.

a  $\frac{1}{3-\sqrt{5}}$

b  $\frac{2}{4+\sqrt{3}}$

c  $\frac{6}{5-\sqrt{2}}$

3 Rationalise and simplify, if possible.

a  $\frac{1}{\sqrt{9}-\sqrt{8}}$

b  $\frac{1}{\sqrt{x}-\sqrt{y}}$

Solutions

## Straight Lines

### Worked Examples

Work out the gradient of the line joining (2, 4) and (8, 7).

$x_1 = 2, x_2 = 8, y_1 = 4$ and $y_2 = 7$ $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{7 - 4}{8 - 2} = \frac{3}{6} = \frac{1}{2}$ $m = \frac{1}{2}$	Substitute the coordinates into the equation $m = \frac{y_2 - y_1}{x_2 - x_1}$ to work out the gradient of the line.
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Find the equation of the line which passes through the point (5, 13) and has gradient 3.

$m = 3$ $y = 3x + c$ $13 = 3 \times 5 + c$ $13 = 15 + c$ $c = -2$ $y = 3x - 2$	<ol style="list-style-type: none"><li>1 Substitute the gradient given in the question into the equation of a straight line <math>y = mx + c</math>.</li><li>2 Substitute the coordinates <math>x = 5</math> and <math>y = 13</math> into the equation.</li><li>3 Simplify and solve the equation.</li><li>4 Substitute <math>c = -2</math> into the equation <math>y = 3x + c</math></li></ol>
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Find the equation of the line passing through the points with coordinates (2, 4) and (8, 7).

$x_1 = 2, x_2 = 8, y_1 = 4$ and $y_2 = 7$ $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{7 - 4}{8 - 2} = \frac{3}{6} = \frac{1}{2}$ $y = \frac{1}{2}x + c$ $4 = \frac{1}{2} \times 2 + c$ $c = 3$ $y = \frac{1}{2}x + 3$	<ol style="list-style-type: none"><li>1 Substitute the coordinates into the equation <math>m = \frac{y_2 - y_1}{x_2 - x_1}</math> to work out the gradient of the line.</li><li>2 Substitute the gradient into the equation of a straight line <math>y = mx + c</math>.</li><li>3 Substitute the coordinates of either point into the equation.</li><li>4 Simplify and solve the equation.</li><li>5 Substitute <math>c = 3</math> into the equation <math>y = \frac{1}{2}x + c</math></li></ol>
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Find the equation of the line parallel to  $y = 2x + 4$  which passes through the point (4, 9).

$y = 2x + 4$ $m = 2$ $y = 2x + c$ $9 = 2 \times 4 + c$ $9 = 8 + c$ $c = 1$ $y = 2x + 1$	<ol style="list-style-type: none"><li>1 As the lines are parallel they have the same gradient.</li><li>2 Substitute <math>m = 2</math> into the equation of a straight line <math>y = mx + c</math>.</li><li>3 Substitute the coordinates into the equation <math>y = 2x + c</math></li><li>4 Simplify and solve the equation.</li><li>5 Substitute <math>c = 1</math> into the equation <math>y = 2x + c</math></li></ol>
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## Practice Questions

Set 1

Work out the gradient of the line joining  $(-2, 7)$  and  $(4, 5)$

Set 2

Find the equation of the line with gradient 5 that passes through the point  $(3, 2)$ .

Set 3

Find the equation of the line that passes through the points  $(5, 7)$  and  $(3, -1)$ .

Set 4

A line is parallel to the line  $6x + 3y - 2 = 0$  and it passes through the point  $(0, 3)$ . Work out the equation of the line.

## Video Solutions

[Set 1](#)

[Set 2](#)

[Set 3](#)

[Set 4](#)

## Additional Practice

Set 1

**1** Work out the gradient of the line joining each pair of coordinates.

**a**  $(4, 5), (10, 17)$

**b**  $(0, 6), (-4, 8)$

**c**  $(-1, -7), (5, 23)$

**d**  $(3, 10), (4, 7)$

Set 2 **1** Find, in the form  $ax + by + c = 0$  where  $a, b$  and  $c$  are integers, an equation for each of the lines with the following gradients and  $y$ -intercepts.

**a** gradient  $-\frac{1}{2}$ ,  $y$ -intercept  $-7$

**b** gradient  $2$ ,  $y$ -intercept  $0$

**c** gradient  $\frac{2}{3}$ ,  $y$ -intercept  $4$

**d** gradient  $-1.2$ ,  $y$ -intercept  $-2$

**2** Write an equation for the line which passes through the point  $(2, 5)$  and has gradient  $4$ .

**3** Write an equation for the line which passes through the point  $(6, 3)$  and has gradient  $-\frac{2}{3}$

Set 3

**1** Write an equation for the line passing through each of the following pairs of points.

**a**  $(4, 5), (10, 17)$

**b**  $(0, 6), (-4, 8)$

**c**  $(-1, -7), (5, 23)$

**d**  $(3, 10), (4, 7)$

Set 4

**1** Find the equation of the line parallel to each of the given lines and which passes through each of the given points.

**a**  $y = 3x + 1$   $(3, 2)$

**b**  $y = 3 - 2x$   $(1, 3)$

**c**  $2x + 4y + 3 = 0$   $(6, -3)$

**d**  $2y - 3x + 2 = 0$   $(8, 20)$

[Solutions](#)

## Algebraic Methods

### Worked Examples

Factorise  $x^2 + 3x - 10$

$b = 3, ac = -10$  So $x^2 + 3x - 10 = x^2 + 5x - 2x - 10$ $= x(x + 5) - 2(x + 5)$ $= (x + 5)(x - 2)$	<ol style="list-style-type: none"><li>1 Work out the two factors of <math>ac = -10</math> which add to give <math>b = 3</math> (5 and -2)</li><li>2 Rewrite the <math>b</math> term (<math>3x</math>) using these two factors</li><li>3 Factorise the first two terms and the last two terms</li><li>4 <math>(x + 5)</math> is a factor of both terms</li></ol>
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Factorise  $6x^2 - 11x - 10$

$b = -11, ac = -60$  So $6x^2 - 11x - 10 = 6x^2 - 15x + 4x - 10$ $= 3x(2x - 5) + 2(2x - 5)$ $= (2x - 5)(3x + 2)$	<ol style="list-style-type: none"><li>1 Work out the two factors of <math>ac = -60</math> which add to give <math>b = -11</math> (-15 and 4)</li><li>2 Rewrite the <math>b</math> term (<math>-11x</math>) using these two factors</li><li>3 Factorise the first two terms and the last two terms</li><li>4 <math>(2x - 5)</math> is a factor of both terms</li></ol>
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Factorise  $4x^2 - 25y^2$

$4x^2 - 25y^2 = (2x + 5y)(2x - 5y)$	This is the difference of two squares as the two terms can be written as $(2x)^2$ and $(5y)^2$
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Simplify  $\frac{x^2 - 4x - 21}{2x^2 + 9x + 9}$

$\frac{x^2 - 4x - 21}{2x^2 + 9x + 9}$ <p>For the numerator: <math>b = -4, ac = -21</math></p> <p>So <math>x^2 - 4x - 21 = x^2 - 7x + 3x - 21</math></p> $= x(x - 7) + 3(x - 7)$ $= (x - 7)(x + 3)$ <p>For the denominator: <math>b = 9, ac = 18</math></p> <p>So <math>2x^2 + 9x + 9 = 2x^2 + 6x + 3x + 9</math></p> $= 2x(x + 3) + 3(x + 3)$ $= (x + 3)(2x + 3)$ <p>So <math>\frac{x^2 - 4x - 21}{2x^2 + 9x + 9} = \frac{(x - 7)(x + 3)}{(x + 3)(2x + 3)}</math></p> $= \frac{x - 7}{2x + 3}$	<ol style="list-style-type: none"> <li>1 Factorise the numerator and the denominator</li> <li>2 Work out the two factors of <math>ac = -21</math> which add to give <math>b = -4</math> (<math>-7</math> and <math>3</math>)</li> <li>3 Rewrite the <math>b</math> term (<math>-4x</math>) using these two factors</li> <li>4 Factorise the first two terms and the last two terms</li> <li>5 <math>(x - 7)</math> is a factor of both terms</li> <li>6 Work out the two factors of <math>ac = 18</math> which add to give <math>b = 9</math> (<math>6</math> and <math>3</math>)</li> <li>7 Rewrite the <math>b</math> term (<math>9x</math>) using these two factors</li> <li>8 Factorise the first two terms and the last two terms</li> <li>9 <math>(x + 3)</math> is a factor of both terms</li> <li>10 <math>(x + 3)</math> is a factor of both the numerator and denominator so cancels out as a value divided by itself is 1</li> </ol>
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### Practice Questions

Set 1

Simplify these fractions:

a.  $\frac{7x^4 - 2x^3 + 6x}{x}$

b.  $\frac{(x + 7)(2x - 1)}{(2x - 1)}$

c.  $\frac{x^2 + 7x + 12}{(x + 3)}$

d.  $\frac{x^2 + 6x + 5}{x^2 + 3x - 10}$

e.  $\frac{2x^2 + 11x + 12}{(x + 3)(x + 4)}$

## Video Solutions

### Set 1

## Additional Practice

### Set 1

**1** Simplify the algebraic fractions.

**a**  $\frac{2x^2 + 4x}{x^2 - x}$

**b**  $\frac{x^2 + 3x}{x^2 + 2x - 3}$

**c**  $\frac{x^2 - 2x - 8}{x^2 - 4x}$

**d**  $\frac{x^2 - 5x}{x^2 - 25}$

**e**  $\frac{x^2 - x - 12}{x^2 - 4x}$

**f**  $\frac{2x^2 + 14x}{2x^2 + 4x - 70}$

**2** Simplify

**a**  $\frac{9x^2 - 16}{3x^2 + 17x - 28}$

**b**  $\frac{2x^2 - 7x - 15}{3x^2 - 17x + 10}$

## Solutions

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## Quadratic Equations

### Worked Examples

Solve  $5x^2 = 15x$

$5x^2 = 15x$ $5x^2 - 15x = 0$ $5x(x - 3) = 0$ So $5x = 0$ or $(x - 3) = 0$ Therefore $x = 0$ or $x = 3$	<ol style="list-style-type: none"><li>1 Rearrange the equation so that all of the terms are on one side of the equation and it is equal to zero. Do not divide both sides by <math>x</math> as this would lose the solution <math>x = 0</math>.</li><li>2 Factorise the quadratic equation. <math>5x</math> is a common factor.</li><li>3 When two values multiply to make zero, at least one of the values must be zero.</li><li>4 Solve these two equations.</li></ol>
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Solve  $x^2 + 7x + 12 = 0$

$x^2 + 7x + 12 = 0$ $b = 7, ac = 12$ $x^2 + 4x + 3x + 12 = 0$ $x(x + 4) + 3(x + 4) = 0$ $(x + 4)(x + 3) = 0$ So $(x + 4) = 0$ or $(x + 3) = 0$ Therefore $x = -4$ or $x = -3$	<ol style="list-style-type: none"><li>1 Factorise the quadratic equation. Work out the two factors of <math>ac = 12</math> which add to give you <math>b = 7</math>. (4 and 3)</li><li>2 Rewrite the <math>b</math> term (<math>7x</math>) using these two factors.</li><li>3 Factorise the first two terms and the last two terms.</li><li>4 <math>(x + 4)</math> is a factor of both terms.</li><li>5 When two values multiply to make zero, at least one of the values must be zero.</li><li>6 Solve these two equations.</li></ol>
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Solve  $3x^2 - 7x - 2 = 0$ . Give your solutions in surd form.

$a = 3, b = -7, c = -2$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(3)(-2)}}{2(3)}$ $x = \frac{7 \pm \sqrt{73}}{6}$ So $x = \frac{7 - \sqrt{73}}{6}$ or $x = \frac{7 + \sqrt{73}}{6}$	<ol style="list-style-type: none"><li>1 Identify <math>a, b</math> and <math>c</math>, making sure you get the signs right and write down the formula. Remember that <math>-b \pm \sqrt{b^2 - 4ac}</math> is all over <math>2a</math>, not just part of it.</li><li>2 Substitute <math>a = 3, b = -7, c = -2</math> into the formula.</li><li>3 Simplify. The denominator is 6 when <math>a = 3</math>. A common mistake is to always write a denominator of 2.</li><li>4 Write down both the solutions.</li></ol>
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Complete the square for the expression  $x^2 + 6x$

$x^2 + 6x$ $= \left(x + \frac{6}{2}\right)^2 - \left(\frac{6}{2}\right)^2$ $= (x + 3)^2 - 9$	<p><b>1</b> Write <math>x^2 + bx + c</math> in the form <math>\left(x + \frac{b}{2}\right)^2 - \left(\frac{b}{2}\right)^2 + c</math></p> <p><b>2</b> Simplify.</p>
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Complete the square for the expression  $2x^2 - 7x$

$2x^2 - 7x$ $= 2\left(x^2 - \frac{7}{2}x\right)$ $= 2\left[\left(x - \frac{7}{4}\right)^2 - \left(\frac{7}{4}\right)^2\right]$ $= 2\left(x - \frac{7}{4}\right)^2 - \frac{49}{8}$	<p><b>1</b> Before completing the square write <math>ax^2 + bx + c</math> in the form <math>a\left(x^2 + \frac{b}{a}x\right) + c</math></p> <p><b>2</b> Now complete the square by writing <math>x^2 - \frac{7}{2}x</math> in the form <math>\left(x + \frac{b}{2a}\right)^2 - \left(\frac{b}{2a}\right)^2</math></p> <p><b>3</b> Expand and Simplify</p>
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Solve  $x^2 + 6x + 4 = 0$ . Give your solutions in surd form.

$x^2 + 6x + 4 = 0$ $(x + 3)^2 - 9 + 4 = 0$ $(x + 3)^2 - 5 = 0$ $(x + 3)^2 = 5$ $x + 3 = \pm\sqrt{5}$ $x = \pm\sqrt{5} - 3$ $\text{So } x = -\sqrt{5} - 3 \text{ or } x = \sqrt{5} - 3$	<p><b>1</b> Write <math>x^2 + bx + c = 0</math> in the form <math>\left(x + \frac{b}{2}\right)^2 - \left(\frac{b}{2}\right)^2 + c = 0</math></p> <p><b>2</b> Simplify.</p> <p><b>3</b> Rearrange the equation to work out <math>x</math>. First, add 5 to both sides.</p> <p><b>4</b> Square root both sides. Remember that the square root of a value gives two answers.</p> <p><b>5</b> Subtract 3 from both sides to solve the equation.</p> <p><b>6</b> Write down both solutions.</p>
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## Practice Questions

Set 1

Solve the following equations:

**a.**  $x^2 - 2x - 15 = 0$       **b.**  $x^2 = 9x$       **c.**  $6x^2 + 13x - 5 = 0$

**d.**  $x^2 - 5x + 18 = 2 + 3x$

Set 2

Solve  $3x^2 - 7x - 1 = 0$  by using the formula.

Set 3

Complete the square for the expressions:

**a.**  $x^2 + 8x$

**b.**  $x^2 - 3x$

**c.**  $2x^2 - 12x$

Set 4

Solve the equation  $x^2 + 8x + 10 = 0$  by completing the square.

Give your answers in surd form.

## Video Solutions

[Set 1](#)

[Set 2](#)

[Set 3](#)

[Set 4](#)

## Additional Practice

Set 1

**1** Solve

**a**  $6x^2 + 4x = 0$

**b**  $28x^2 - 21x = 0$

**c**  $x^2 + 7x + 10 = 0$

**d**  $x^2 - 5x + 6 = 0$

**e**  $x^2 - 3x - 4 = 0$

**f**  $x^2 + 3x - 10 = 0$

**g**  $2x^2 - 7x - 4 = 0$

**h**  $3x^2 - 13x - 10 = 0$

Set 2

1 Solve, giving your solutions in surd form.

**a**  $3x^2 + 6x + 2 = 0$

**b**  $2x^2 - 4x - 7 = 0$

2 Solve the equation  $x^2 - 7x + 2 = 0$

Give your solutions in the form  $\frac{a \pm \sqrt{b}}{c}$ , where  $a$ ,  $b$  and  $c$  are integers.

3 Solve  $10x^2 + 3x + 3 = 5$

Give your solution in surd form.

Set 3

1 Complete the square for the following expressions:

**a**  $x^2 + 8x$

**b**  $x^2 - 10x$

**c**  $x^2 - x$

**d**  $3x^2 - 15x$

Set 4

1 Solve by completing the square.

**a**  $x^2 - 4x - 3 = 0$

**b**  $x^2 - 10x + 4 = 0$

**c**  $x^2 + 8x - 5 = 0$

**d**  $x^2 - 2x - 6 = 0$

[Solutions](#)

## Simultaneous Equations

### Worked Examples

Solve the simultaneous equations  $3x + y = 5$  and  $x + y = 1$

$\begin{array}{r} 3x + y = 5 \\ - \quad x + y = 1 \\ \hline 2x \quad = 4 \end{array}$ <p>So <math>x = 2</math></p> <p>Using <math>x + y = 1</math> <math>2 + y = 1</math> So <math>y = -1</math></p> <p>Check: equation 1: <math>3 \times 2 + (-1) = 5</math> YES equation 2: <math>2 + (-1) = 1</math> YES</p>	<ol style="list-style-type: none"><li>1 Subtract the second equation from the first equation to eliminate the <math>y</math> term.</li><li>2 To find the value of <math>y</math>, substitute <math>x = 2</math> into one of the original equations.</li><li>3 Substitute the values of <math>x</math> and <math>y</math> into both equations to check your answers.</li></ol>
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Solve  $x + 2y = 13$  and  $5x - 2y = 5$  simultaneously.

$\begin{array}{r} x + 2y = 13 \\ + \quad 5x - 2y = 5 \\ \hline 6x \quad = 18 \end{array}$ <p>So <math>x = 3</math></p> <p>Using <math>x + 2y = 13</math> <math>3 + 2y = 13</math> So <math>y = 5</math></p> <p>Check: equation 1: <math>3 + 2 \times 5 = 13</math> YES equation 2: <math>5 \times 3 - 2 \times 5 = 5</math> YES</p>	<ol style="list-style-type: none"><li>1 Add the two equations together to eliminate the <math>y</math> term.</li><li>2 To find the value of <math>y</math>, substitute <math>x = 3</math> into one of the original equations.</li><li>3 Substitute the values of <math>x</math> and <math>y</math> into both equations to check your answers.</li></ol>
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Solve the simultaneous equations  $y = 2x - 1$  and  $y = x^2 - 4$

$2x - 1 = x^2 - 4$ $x^2 - 2x - 3 = 0$ $(x+1)(x-3) = 0$ $x = -1 \text{ and } x = 3$ $x = -1, y = -3$ $x = 3, y = 5$ <p>Check:</p> <p>Equation 1: <math>-3 = 2(-1) - 1</math>    YES  <math>5 = 2(3) - 1</math>    YES</p> <p>Equation 2: <math>-1 = (-1)^2 - 4</math>    YES  <math>5 = (3)^2 - 4</math>    YES</p>	<ol style="list-style-type: none"> <li>1 Substitute <math>2x - 1</math> for <math>y</math> in the linear equation</li> <li>2 Rearrange to obtain a quadratic equation whose RHS is zero</li> <li>3 Factorize</li> <li>4 Find two values for <math>x</math></li> <li>5 Substitute each of these values in turn into the other equation to find two values for <math>y</math></li> <li>6 Substitute both values for <math>x</math> and <math>y</math> into both equations to check your answers.</li> </ol>
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Solve simultaneously,  $y = x + 1$  and  $y = 1 + \frac{4}{x}$

$x + 1 = 1 + \frac{4}{x}$ $x^2 + x = x + 4$ $x^2 - 4 = 0$ $(x - 2)(x + 2) = 0$ $x = 2 \text{ and } x = -2$ $x = 2, y = 3$ $x = -2, y = -1$ <p>Check:</p> <p>Equation 1: <math>3 = 2 + 1</math>    YES  <math>-1 = -2 + 1</math>          YES</p> <p>Equation 2: <math>3 = 1 + (4 \div 2)</math>    YES  <math>-1 = 1 + (4 \div (-2))</math>    YES</p>	<ol style="list-style-type: none"> <li>1 Substitute <math>x + 1</math> for <math>y</math> in the linear equation</li> <li>2 Multiply both sides by <math>x</math></li> <li>3 Rearrange to obtain a quadratic equation whose RHS is zero</li> <li>3 Factorize</li> <li>4 Find two values for <math>x</math></li> <li>5 Substitute each of these values in turn into the other equation to find two values for <math>y</math></li> <li>6 Substitute both values for <math>x</math> and <math>y</math> into both equations to check your answers.</li> </ol>
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## Practice Questions

Set 1

Solve the simultaneous equations:

**a.**  $2x + 3y = 8$   
 $3x - y = 23$

**b.**  $4x - 5y = 4$   
 $6x + 2y = 25$

Set 2

Solve the simultaneous equations:

$$2x + 2y = 3$$
$$x^2 + 3xy = 10$$

## Video Solutions

[Set 1](#)

[Set 2](#)

## Additional Practice

Set 1

**1**  $4x + y = 8$   
 $x + y = 5$

**2**  $3x + y = 7$   
 $3x + 2y = 5$

**3**  $4x + y = 3$   
 $3x - y = 11$

**4**  $3x + 4y = 7$   
 $x - 4y = 5$

**5**  $2x + y = 11$   
 $x - 3y = 9$

**6**  $2x + 3y = 11$   
 $3x + 2y = 4$

Set 2

Solve these simultaneous equations.

**1**  $xy = 9$  and  $y = x$

**2**  $x^2 + y^2 = 50$  and  $y = x$

**3**  $xy - 3 = 16$  and  $x - 19y = 0$

## Solutions

## Inequalities

### Worked Examples

Solve  $2x - 5 < 7$

$2x - 5 < 7$ $2x < 12$ $x < 6$	<ol style="list-style-type: none"><li>1 Add 5 to both sides.</li><li>2 Divide both sides by 2.</li></ol>
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Solve  $2 - 5x \geq -8$

$2 - 5x \geq -8$ $-5x \geq -10$ $x \leq 2$	<ol style="list-style-type: none"><li>1 Subtract 2 from both sides.</li><li>2 Divide both sides by <math>-5</math>. Remember to reverse the inequality when dividing by a negative number.</li></ol>
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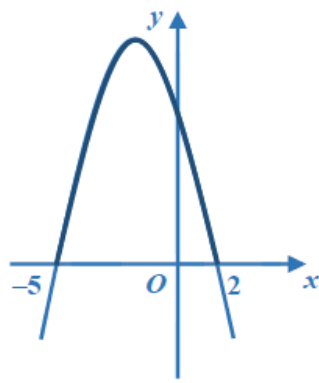
Solve  $4(x - 2) > 3(9 - x)$

$4(x - 2) > 3(9 - x)$ $4x - 8 > 27 - 3x$ $7x - 8 > 27$ $7x > 35$ $x > 5$	<ol style="list-style-type: none"><li>1 Expand the brackets.</li><li>2 Add <math>3x</math> to both sides.</li><li>3 Add 8 to both sides.</li><li>4 Divide both sides by 7.</li></ol>
--	--

Find the set of values of  $x$  which satisfy  $x^2 + 5x + 6 > 0$

$x^2 + 5x + 6 = 0$ $(x + 3)(x + 2) = 0$ $x = -3 \text{ or } x = -2$ <p>It is above the <math>x</math>-axis where <math>x^2 + 5x + 6 &gt; 0</math></p> <p>This part of the graph is not needed as this is where <math>x^2 + 5x + 6 &lt; 0</math></p> $x < -3 \text{ or } x > -2$	<ol style="list-style-type: none"><li>1 Solve the quadratic equation by factorising.</li><li>2 Sketch the graph of <math>y = (x + 3)(x + 2)</math></li><li>3 Identify on the graph where <math>x^2 + 5x + 6 &gt; 0</math>, i.e. where <math>y &gt; 0</math></li><li>4 Write down the values which satisfy the inequality <math>x^2 + 5x + 6 &gt; 0</math></li></ol>
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Find the set of values of  $x$  which satisfy  $-x^2 - 3x + 10 \geq 0$

<p><math>-x^2 - 3x + 10 = 0</math> <math>(-x + 2)(x + 5) = 0</math> <math>x = 2</math> or <math>x = -5</math></p>  <p><math>-5 \leq x \leq 2</math></p>	<ol style="list-style-type: none"><li>1 Solve the quadratic equation by factorising.</li><li>2 Sketch the graph of <math>y = (-x + 2)(x + 5) = 0</math></li><li>3 Identify on the graph where <math>-x^2 - 3x + 10 \geq 0</math>, i.e. where <math>y \geq 0</math></li><li>3 Write down the values which satisfy the inequality <math>-x^2 - 3x + 10 \geq 0</math></li></ol>
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### Practice Questions

Set 1

Find the set of values of  $x$  for which:

**a.**  $5x + 9 \geq x + 20$

**b.**  $12 - 3x < 27$

**c.**  $3(x - 5) > 5 - 2(x - 8)$

Set 2

Find the set of values of  $x$  for which:

$3 - 5x - 2x^2 < 0$

### Video Solutions

[Set 1](#)

[Set 2](#)



## Additional Practice

Set 1

**1** Solve

**a**  $2 - 4x \geq 18$

**b**  $3 \leq 7x + 10 < 45$

**c**  $6 - 2x \geq 4$

**d**  $4x + 17 < 2 - x$

**e**  $4 - 5x < -3x$

**f**  $-4x \geq 24$

**2** Solve these inequalities

**a**  $3t + 1 < t + 6$

**b**  $2(3n - 1) \geq n + 5$

**3** Solve

**a**  $3(2 - x) > 2(4 - x) + 4$

**b**  $5(4 - x) > 3(5 - x) + 2$

Set 2

**1** Find the set of values of  $x$  for which  $(x + 7)(x - 4) \leq 0$

**2** Find the set of values of  $x$  for which  $x^2 - 4x - 12 \geq 0$

**3** Find the set of values of  $x$  for which  $2x^2 - 7x + 3 < 0$

**4** Find the set of values of  $x$  for which  $4x^2 + 4x - 3 > 0$

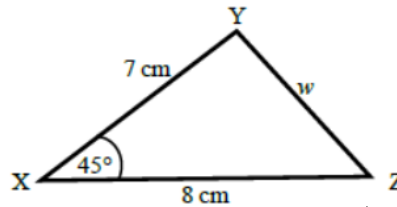
**5** Find the set of values of  $x$  for which  $12 + x - x^2 \geq 0$

## Solutions

# Trigonometry

## Worked Examples

Work out the length of side  $w$ .  
Give your answer correct to 3 significant figures.



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$w^2 = 8^2 + 7^2 - 2 \times 8 \times 7 \times \cos 45^\circ$$

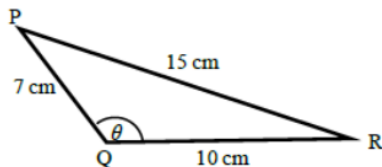
$$w^2 = 33.804\ 040\ 51\dots$$

$$w = \sqrt{33.804\ 040\ 51}$$

$$w = 5.81\ \text{cm}$$

- 1 Always start by labelling the angles and sides.
- 2 Write the cosine rule to find the side.
- 3 Substitute the values  $a$ ,  $b$  and  $A$  into the formula.
- 4 Use a calculator to find  $w^2$  and then  $w$ .
- 5 Round your final answer to 3 significant figures and write the units in your answer.

Work out the size of angle  $\theta$ .  
Give your answer correct to 1 decimal place.



$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos \theta = \frac{10^2 + 7^2 - 15^2}{2 \times 10 \times 7}$$

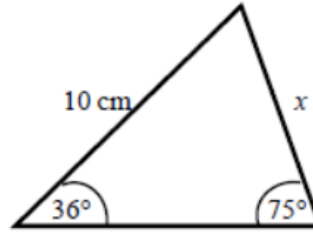
$$\cos \theta = \frac{-76}{140}$$

$$\theta = 122.878\ 349\dots$$

$$\theta = 122.9^\circ$$

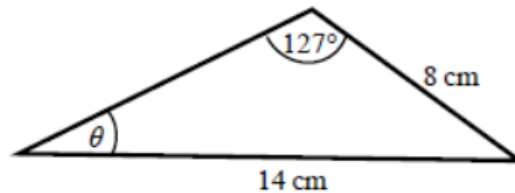
- 1 Always start by labelling the angles and sides.
- 2 Write the cosine rule to find the angle.
- 3 Substitute the values  $a$ ,  $b$  and  $c$  into the formula.
- 4 Use  $\cos^{-1}$  to find the angle.
- 5 Use your calculator to work out  $\cos^{-1}(-76 \div 140)$ .
- 6 Round your answer to 1 decimal place and write the units in your answer.

Work out the length of side  $x$ .  
Give your answer correct to 3 significant figures.



$\frac{a}{\sin A} = \frac{b}{\sin B}$ $\frac{x}{\sin 36^\circ} = \frac{10}{\sin 75^\circ}$ $x = \frac{10 \times \sin 36^\circ}{\sin 75^\circ}$ $x = 6.09 \text{ cm}$	<ol style="list-style-type: none"> <li>1 Always start by labelling the angles and sides.</li> <li>2 Write the sine rule to find the side.</li> <li>3 Substitute the values <math>a</math>, <math>b</math>, <math>A</math> and <math>B</math> into the formula.</li> <li>4 Rearrange to make <math>x</math> the subject.</li> <li>5 Round your answer to 3 significant figures and write the units in your answer.</li> </ol>
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Work out the size of angle  $\theta$ .  
Give your answer correct to 1 decimal place.



$\frac{\sin A}{a} = \frac{\sin B}{b}$ $\frac{\sin \theta}{8} = \frac{\sin 127^\circ}{14}$ $\sin \theta = \frac{8 \times \sin 127^\circ}{14}$ $\theta = 27.2^\circ$	<ol style="list-style-type: none"> <li>1 Always start by labelling the angles and sides.</li> <li>2 Write the sine rule to find the angle.</li> <li>3 Substitute the values <math>a</math>, <math>b</math>, <math>A</math> and <math>B</math> into the formula.</li> <li>4 Rearrange to make <math>\sin \theta</math> the subject.</li> <li>5 Use <math>\sin^{-1}</math> to find the angle. Round your answer to 1 decimal place and write the units in your answer.</li> </ol>
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## Practice Questions

Set 1

Calculate the length of the side  $AB$  of the triangle  $ABC$  in which  $AC = 6.5$  cm,  $BC = 8.7$  cm and  $\angle ACB = 100^\circ$ .

Set 2

Find the size of the smallest angle in a triangle whose sides have lengths 3 cm, 5 cm and 6 cm.

Set 3

In  $\triangle ABC$ ,  $AB = 8$  cm,  $\angle BAC = 30^\circ$  and  $\angle BCA = 40^\circ$ . Find  $BC$ .

Set 4

In  $\triangle ABC$ ,  $AB = 3.8$  cm,  $BC = 5.2$  cm and  $\angle BAC = 35^\circ$ . Find  $\angle ABC$ .

Set 5

- a. Sketch the graph of  $y = \cos \theta$  in the interval  $-360^\circ \leq \theta \leq 360^\circ$ .
- b. i. Sketch the graph of  $y = \sin x$  in the interval  $-180^\circ \leq x \leq 270^\circ$ 
  - ii.  $\sin(-30^\circ) = -0.5$ . Use your graph to determine two further values of  $x$  for which  $\sin x = -0.5$ .

## Video Solutions

[Set 1](#)

[Set 2](#)

[Set 3](#)

[Set 4](#)

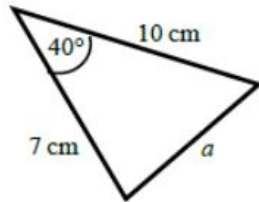
[Set 5](#)

## Additional Practice

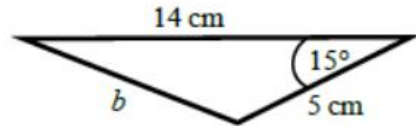
### Set 1

- 1 Work out the length of the unknown side in each triangle.  
Give your answers correct to 3 significant figures.

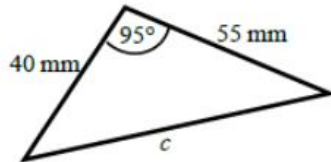
a



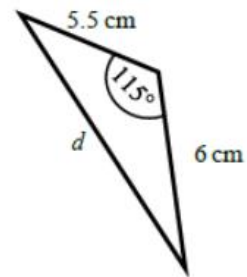
b



c



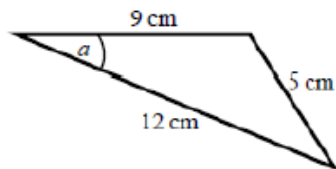
d



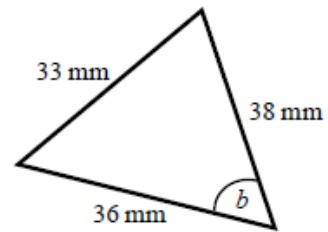
### Set 2

- 1 Calculate the angles labelled  $\theta$  in each triangle.  
Give your answer correct to 1 decimal place.

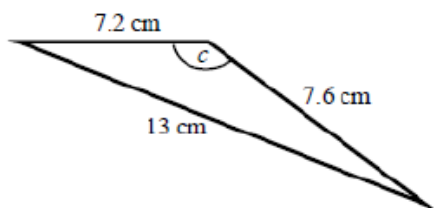
a



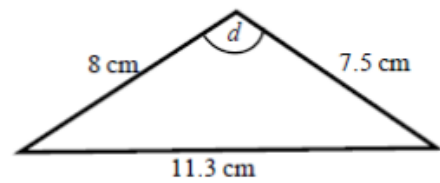
b



c

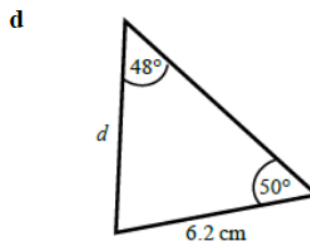
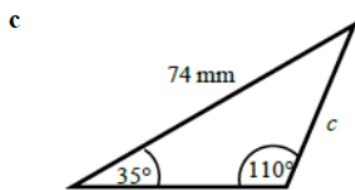
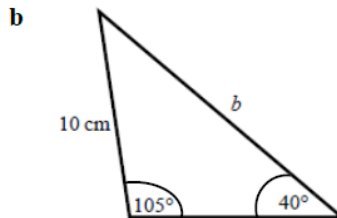
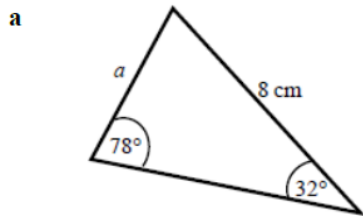


d



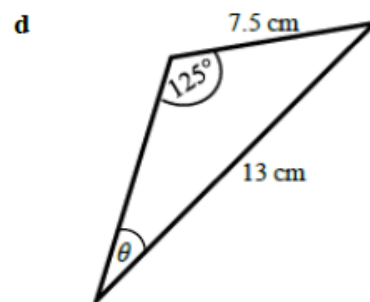
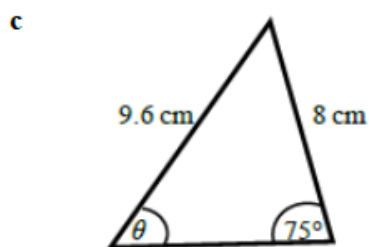
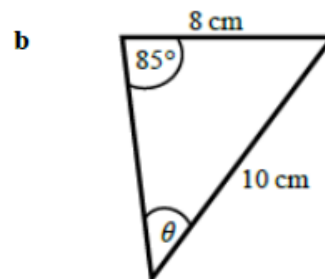
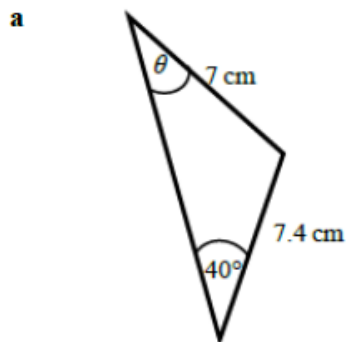
Set 3

- 1 Find the length of the unknown side in each triangle. Give your answers correct to 3 significant figures.



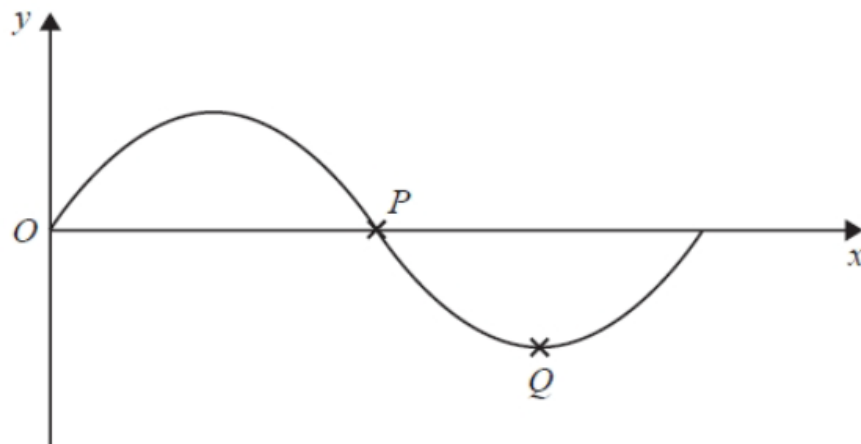
Set 4

- 1 Calculate the angles labelled  $\theta$  in each triangle. Give your answer correct to 1 decimal place.



Set 5

1 The diagram shows part of a sketch of the curve  $y = \sin x^\circ$



(a) Write down the coordinates of

(i) the point  $P$

( ..... , ..... )

(ii) the point  $Q$

( ..... , ..... )

(b) Sketch the graph of  $y = \tan x$  for  $0^\circ \leq x \leq 360^\circ$

Show the coordinates of any points of intersection with the coordinate axes.

Solutions

## Solutions

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### Indices

#### Additional Practice

Set 1

- |           |               |           |                  |
|-----------|---------------|-----------|------------------|
| <b>1.</b> | (a) $a^9$     | <b>2.</b> | (a) $x^{10}$     |
|           | (b) $9e^5f^6$ |           | (b) $m^{12}$     |
|           | (c) 3         |           | (c) $3a^{-4}f^6$ |

Set 2

- |          |          |                   |          |                  |
|----------|----------|-------------------|----------|------------------|
| <b>1</b> | <b>a</b> | $\frac{3x^3}{2}$  | <b>b</b> | $5x^2$           |
|          | <b>c</b> | $3x$              | <b>d</b> | $\frac{y}{2x^2}$ |
|          | <b>e</b> | $y^{\frac{1}{2}}$ | <b>f</b> | $c^{-3}$         |
|          | <b>g</b> | $2x^6$            | <b>h</b> | $x$              |

Set 3

- |          |          |                |          |                |
|----------|----------|----------------|----------|----------------|
| <b>1</b> | <b>a</b> | 7              | <b>b</b> | 4              |
| <b>2</b> | <b>a</b> | 125            | <b>b</b> | 32             |
| <b>3</b> | <b>a</b> | $\frac{1}{25}$ | <b>b</b> | $\frac{1}{64}$ |
| <b>4</b> | <b>a</b> | $\frac{1}{2}$  | <b>b</b> | $\frac{1}{9}$  |



## Surds

### Additional Practice

#### Set 1

1 a  $3\sqrt{5}$

c  $4\sqrt{3}$

2 a  $15\sqrt{2}$

c  $3\sqrt{2}$

e  $6\sqrt{7}$

b  $5\sqrt{5}$

d  $5\sqrt{7}$

b  $\sqrt{5}$

d  $\sqrt{3}$

f  $5\sqrt{3}$

#### Set 2

1 a  $-1$

c  $10\sqrt{5}-7$

2  $x-y$

3  $18$

4  $1+2\sqrt{2}$

b  $9-\sqrt{3}$

d  $26-4\sqrt{2}$

#### Set 3

1 a  $\frac{\sqrt{5}}{5}$

c  $\frac{2\sqrt{7}}{7}$

e  $\sqrt{2}$

2 a  $\frac{3+\sqrt{5}}{4}$

3 a  $3+2\sqrt{2}$

b  $\frac{\sqrt{11}}{11}$

d  $\frac{\sqrt{2}}{2}$

f  $\sqrt{5}$

b  $\frac{2(4-\sqrt{3})}{13}$

b  $\frac{\sqrt{x}+\sqrt{y}}{x-y}$

c  $\frac{6(5+\sqrt{2})}{23}$

## Straight Lines

### Additional Practice

Set 1

**1 a**  $m = 2$                       **b**  $m = -\frac{1}{2}$

**c**  $m = 5$                       **d**  $m = -3$

Set 2

**1 a**  $x + 2y + 14 = 0$               **b**  $2x - y = 0$

**c**  $2x - 3y + 12 = 0$               **d**  $6x + 5y + 10 = 0$

**2**  $y = 4x - 3$

**3**  $y = -\frac{2}{3}x + 7$

Set 3

**1 a**  $y = 2x - 3$                       **b**  $y = -\frac{1}{2}x + 6$

**c**  $y = 5x - 2$                       **d**  $y = -3x + 19$

Set 4

**1 a**  $y = 3x - 7$                       **b**  $y = -2x + 5$

**c**  $y = -\frac{1}{2}x$                       **d**  $y = \frac{3}{2}x + 8$

Algebraic Methods  
Additional Practice

Set 1

**1 a**  $\frac{2(x+2)}{x-1}$

**c**  $\frac{x+2}{x}$

**e**  $\frac{x+3}{x}$

**2 a**  $\frac{3x+4}{x+7}$

**b**  $\frac{x}{x-1}$

**d**  $\frac{x}{x+5}$

**f**  $\frac{x}{x-5}$

**b**  $\frac{2x+3}{3x-2}$

## Quadratic Equations

### Additional Practice

#### Set 1

**1 a**  $x = 0$  or  $x = -\frac{2}{3}$

**c**  $x = -5$  or  $x = -2$

**e**  $x = -1$  or  $x = 4$

**g**  $x = -\frac{1}{2}$  or  $x = 4$

**b**  $x = 0$  or  $x = \frac{3}{4}$

**d**  $x = 2$  or  $x = 3$

**f**  $x = -5$  or  $x = 2$

**h**  $x = -\frac{2}{3}$  or  $x = 5$

#### Set 2

**1 a**  $x = -1 + \frac{\sqrt{3}}{3}$  or  $x = -1 - \frac{\sqrt{3}}{3}$

**b**  $x = 1 + \frac{3\sqrt{2}}{2}$  or  $x = 1 - \frac{3\sqrt{2}}{2}$

**2**  $x = \frac{7 + \sqrt{41}}{2}$  or  $x = \frac{7 - \sqrt{41}}{2}$

**3**  $x = \frac{-3 + \sqrt{89}}{20}$  or  $x = \frac{-3 - \sqrt{89}}{20}$

#### Set 3

1

**a**  $(x + 4)^2 - 16$

**b**  $(x - 5)^2 - 25$

**c**  $\left(x - \frac{1}{2}\right)^2 - \frac{1}{4}$

**d**  $3\left(x - \frac{5}{2}\right)^2 - \frac{75}{4}$

**e**  $-2(x - 3)^2 + 18$

#### Set 4

**1 a**  $x = 2 + \sqrt{7}$  or  $x = 2 - \sqrt{7}$

**b**  $x = 5 + \sqrt{21}$  or  $x = 5 - \sqrt{21}$

**c**  $x = -4 + \sqrt{21}$  or  $x = -4 - \sqrt{21}$

**d**  $x = 1 + \sqrt{7}$  or  $x = 1 - \sqrt{7}$

## Simultaneous Equations

### Additional Practice

Set 1

**1**  $x = 1, y = 4$       **4**  $x = 3, y = -\frac{1}{2}$

**2**  $x = 3, y = -2$       **5**  $x = 6, y = -1$

**3**  $x = 2, y = -5$       **6**  $x = -2, y = 5$

Set 2

**1**  $x = -3, y = -3$       and       $x = 3, y = 3$

**2**  $x = -5, y = -5$       and       $x = 5, y = 5$

**3**  $x = -19, y = -1$       and       $x = 19, y = 1$

## Inequalities

### Additional Practice

Set 1

**1 a**  $x \leq -4$

**d**  $x < -3$

**b**  $-1 \leq x < 5$

**e**  $x > 2$

**c**  $x \leq 1$

**f**  $x \leq -6$

**2 a**  $t < \frac{5}{2}$

**b**  $n \geq \frac{7}{5}$

**3**

**a**  $x < -6$

**b**  $x < \frac{3}{2}$

Set 2

**1**  $-7 \leq x \leq 4$

**2**  $x \leq -2$  or  $x \geq 6$

**3**  $\frac{1}{2} < x < 3$

**4**  $x < -\frac{3}{2}$  or  $x > \frac{1}{2}$

**5**  $-3 \leq x \leq 4$

## Trigonometry

### Additional Practice

Set 1

- 1**   **a**   6.46 cm                      **b**   9.26 cm                      **c**   70.8 mm                      **d**   9.70 cm

Set 2

- 1**   **a**   22.2°                      **b**   52.9°                      **c**   122.9°                      **d**   93.6°

Set 3

- 1**   **a**   4.33 cm                      **b**   15.0 cm                      **c**   45.2 mm                      **d**   6.39 cm

Set 4

- 1**   **a**   42.8°                      **b**   52.8°                      **c**   53.6°                      **d**   28.2°

Set 5

- 1**   (a)(i)   (180, 0)  
      (ii)   (270, -1)  
      (b)

